AP Calculus - Final Review Sheet

When you see the words



1. Find the zeros Set function = 0, factor or use quadratic equation if quadratic, graph to find zeros on calculator 2. Find equation of the line tangent to f(x) on [a,b]Take derivative - f'(a) = m and use $y - y_1 = m(x - x_1)$ Same as above but $m = \frac{-1}{f'(a)}$ 3. Find equation of the line normal to f(x) on [a,b]Show that f(-x) = f(x) - symmetric to y-axis 4. Show that f(x) is even Show that f(-x) = -f(x) - symmetric to origin 5. Show that f(x) is odd 6. Find the interval where f(x) is increasing Find f'(x), set both numerator and denominator to zero to find critical points, make sign chart of f'(x)and determine where it is positive. 7. Find interval where the slope of f(x) is increasing Find the derivative of f'(x) = f''(x), set both numerator and denominator to zero to find critical points, make sign chart of f''(x) and determine where it is positive. 8. Find the minimum value of a function Make a sign chart of f'(x), find all relative minimums and plug those values back into f(x) and choose the smallest. 9. Find the minimum slope of a function Make a sign chart of the derivative of f'(x) = f''(x), find all relative minimums and plug those values back into f'(x) and choose the smallest. 10. Find critical values Express f'(x) as a fraction and set both numerator and denominator equal to zero.

This is what you think of doing

Express f''(x) as a fraction and set both numerator and denominator equal to zero. Make sign chart of f''(x) to find where f''(x) changes sign. (+ to – or –

Show that $\lim_{x \to a^{-}} f(x) = \lim_{x \to a^{+}} f(x)$ Show that 1) $\lim_{x \to a} f(x)$ exists $(\lim_{x \to a^{-}} f(x) = \lim_{x \to a^{+}} f(x))$

Do all factor/cancel of f(x) and set denominator = 0

2) f(a) exists

Find $\lim_{x\to\infty} f(x)$ and $\lim_{x\to-\infty} f(x)$

Find $\frac{f(b)-f(a)}{a}$

3) $\lim_{x \to a} f(x) = f(a)$

11. Find inflection points

12. Show that $\lim_{x \to a} f(x)$ exists

13. Show that f(x) is continuous

14. Find vertical asymptotes of f(x)

15. Find horizontal asymptotes of f(x)

16. Find the average rate of change of f(x) on [a,b]

Find $f'(a)$
Find $f'(a)$ $\int_{a}^{b} f(x)dx$ Find $f'(a)$
Find $\frac{a}{b-a}$
Make a sign chart of $f'(x)$, find all relative
maximums and plug those values back into $f(x)$ as
well as finding $f(a)$ and $f(b)$ and choose the largest.
First, be sure that the function is continuous at $x = a$.
Take the derivative of each piece and show that
$\lim_{x \to a^{-}} f'(x) = \lim_{x \to a^{+}} f'(x)$
Find $v(t) = s'(t)$
Find $\int_{a}^{b} v(t) dt$
Find $\frac{\int_{a}^{b} v(t) dt}{b-a} = \frac{s(b) - s(a)}{b-a}$
Find $v(k)$ and $a(k)$. Examine their signs. If both
positive, the particle is speeding up, if different signs, then the particle is slowing down.
$s(t) = \int v(t) dt + C$ Plug in $t = 0$ to find C
Show that f is continuous and differentiable on the
interval. If $f(a) = f(b)$, then find some c in $[a, b]$
such that $f'(c) = 0$.
Show that f is continuous and differentiable on the
interval. Then find some c such that
$f'(c) = \frac{f(b) - f(a)}{b - a}.$
Assume domain is $(-\infty,\infty)$. Restrictable domains:
denominators $\neq 0$, square roots of only non negative
numbers, log or ln of only positive numbers.
Use max/min techniques to rind relative max/mins. Then examine $f(x) f(y)$
Then examine $f(a), f(b)$
Use max/min techniques to rind relative max/mins.
Then examine $\lim_{x\to\pm\infty} f(x)$.
$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$ or
$f'(a) = \lim_{x \to a} \frac{f(x) - f(a)}{x - a}$
Interchange x with y. Solve for $\frac{dy}{dx}$ implicitly (in terms
of y). Plug your x value into the inverse relation and

	solve for y. Finally, plug that y into your $\frac{dy}{dx}$.
	dx
33. y is increasing proportionally to y	$\frac{dy}{dt} = ky \text{ translating to } y = Ce^{kt}$
34. Find the line $x = c$ that divides the area under $f(x)$ on $[a,b]$ to two equal areas	$\int_{a}^{c} f(x)dx = \int_{c}^{b} f(x)dx$
$35. \ \frac{d}{dx} \int_{a}^{x} f(t)dt =$	2^{nd} FTC: Answer is $f(x)$
$36. \frac{d}{dx} \int_{a}^{u} f(t) dt$	2^{nd} FTC: Answer is $f(u)\frac{du}{dx}$
37. The rate of change of population is	$\frac{dP}{dt} = \dots$
38. The line $y = mx + b$ is tangent to $f(x)$ at (x_1, y_1)	Two relationships are true. The two functions share the same slope $(m = f'(x))$ and share the same y value
	at x_1 .
39. Find area using left Riemann sums	$A = base[x_0 + x_1 + x_2 + + x_{n-1}]$
40. Find area using right Riemann sums	$A = base[x_1 + x_2 + x_3 + + x_n]$
41. Find area using midpoint rectangles	Typically done with a table of values. Be sure to use only values that are given. If you are given 6 sets of points, you can only do 3 midpoint rectangles.
42. Find area using trapezoids	$A = \frac{base}{2} \left[x_0 + 2x_1 + 2x_2 + \dots + 2x_{n-1} + x_n \right]$
	This formula only works when the base is the same. If not, you have to do individual trapezoids.
43. Solve the differential equation	Separate the variables $-x$ on one side, y on the other. The dx and dy must all be upstairs.
44. Meaning of $\int_{a}^{x} f(t)dt$	The accumulation function – accumulated area under the function $f(x)$ starting at some constant a and ending at x .
45. Given a base, cross sections perpendicular to the x-axis are squares	The area between the curves typically is the base of your square. So the volume is $\int_{a}^{b} (base^{2}) dx$
46. Find where the tangent line to $f(x)$ is horizontal	Write $f'(x)$ as a fraction. Set the numerator equal to zero.
47. Find where the tangent line to $f(x)$ is vertical	Write $f'(x)$ as a fraction. Set the denominator equal to zero.
48. Find the minimum acceleration given $v(t)$	First find the acceleration $a(t) = v'(t)$. Then minimize
	the acceleration by examining $a'(t)$.
49. Approximate the value of $f(0.1)$ by using the	Find the equation of the tangent line to f using

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tangent line to f at $x = 0$	$y-y_1 = m(x-x_1)$ where $m = f'(0)$ and the point is $(0, f(0))$. Then plug in 0.1 into this line being sure to use an approximate (\approx) sign.
50. Given the value of $F(a)$ and the fact that the anti- derivative of f is F , find $F(b)$ 1	Usually, this problem contains an antiderivative you cannot take. Utilize the fact that if $F(x)$ is the
	antiderivative of f, then $\int_{a}^{b} F(x)dx = F(b) - F(a)$. So
	solve for $F(b)$ using the calculator to find the definite integral.
51. Find the derivative of $f(g(x))$	$f'(g(x))\cdot g'(x)$
52. Given $\int_a^b f(x)dx$, find $\int_a^b [f(x)+k]dx$	$\int_{a}^{b} [f(x) + k] dx = \int_{a}^{b} f(x) dx + \int_{a}^{b} k dx$
53. Given a picture of $f'(x)$, find where $f(x)$ is increasing	Make a sign chart of $f'(x)$ and determine where $f'(x)$ is positive.
54. Given $v(t)$ and $s(0)$, find the greatest distance from the origin of a particle on $[a,b]$	Generate a sign chart of $v(t)$ to find turning points. Then integrate $v(t)$ using $s(0)$ to find the constant to find $s(t)$. Finally, find $s(t)$ turning points which will give you the distance from your starting point. Adjust for the origin.
55. Given a water tank with g gallons initially being filled at the rate of $F(t)$ gallons/min and emptied at the rate of $E(t)$ gallons/min on $[t_1, t_2]$, find a) the amount of water in the tank at m minutes	$g+\int_{t}^{t_{2}}(F(t)-E(t))dt$
56. b) the rate the water amount is changing at m	$\frac{d}{dt}\int_{t}^{m}(F(t)-E(t))dt=F(m)-E(m)$
57. c) the time when the water is at a minimum	F(m)-E(m)=0, testing the endpoints as well.
58. Given a chart of x and $f(x)$ on selected values between a and b , estimate $f'(c)$ where c is between a and b .	Straddle c, using a value k greater than c and a value h less than c. so $f'(c) \approx \frac{f(k) - f(h)}{k - h}$
59. Given $\frac{dy}{dx}$, draw a slope field	Use the given points and plug them into $\frac{dy}{dx}$, drawing
60. Find the area between curves $f(x), g(x)$ on $[a, b]$	little lines with the indicated slopes at the points. $A = \int_{a}^{b} [f(x) - g(x)] dx, \text{ assuming that the } f \text{ curve is}$
	above the g curve.
61. Find the volume if the area between $f(x)g(x)$ is rotated about the x-axis	$A = \pi \int_{a}^{b} \left[f(x)^{2} - g(x)^{2} \right] dx$ assuming that the f curve is above the g curve.